

Optimal Design of WAIMs over Patch Arrays for 5G Applications

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1 SbD Synthesis Tool: implementation and validation

To implement the SbD Synthesis Tool, we used a Particle Swarm Optimizer (PSO). This optimization technique allows to define a swarm of particles that will explore the solution space in order to find the optimal solution. The software is been implemented in order to be able to handle the optimization of single or multiple WAIM layers, composed by both isotropic or anisotropic materials.

1.1 $\epsilon^{sub} = 12.8$ Tests

1.1.1 Test Case #1 - Single Frequency - 1 Isotropic WAIM Layer - $\epsilon^1 = [1 : 5] + j0$ - Square Lattice - $\epsilon^{sub} = 12.8$ Tests

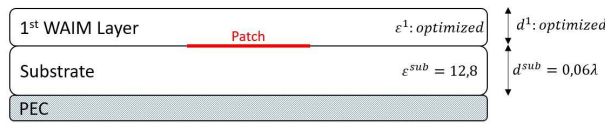


Figure 1: Test Case Schema.

Simulation Parameters:

- Frequency: $f = 10[GHz]$;
- Patch dimensions: $w = 0.15, l = 0.098 [\lambda]$;
- Probe position: $x = 0.049, y = 0.0 [\lambda]$;
- Substrate: $\epsilon_x = 12.8 + j0, \epsilon_y = 12.8 + j0, \epsilon_z = 12.8 + j0, d = 0.06[\lambda]$
- Floquet coefficient = 121;
- Lattice basis: $s_1 = (0.5, 0.0), s_2 = (0.0, 0.5) [\lambda]$;

Analysis Parameters:

- Samples analysis (phi cuts): $\theta \in [0, 90] [deg], \varphi \in [0, 90] [deg], \theta_{samples} = 182, \varphi_{samples} = 3$;
- Samples analysis (3D plots): $\theta \in [-180, 180] [deg], \varphi \in [-90, 90] [deg], \theta_{samples} = 72, \varphi_{samples} = 21$;

PSO Synthesis Parameters:

- Number of WAIM Layers: $N = 1$;
- Unknowns: $U = 2$;
- Unknown ranges: $\epsilon = [1 : 5] + j0, d = [0.033 : 0.5] [\lambda]$;
- Swarm size: $P = 6$;

- Max iteration number: $I = 80$;
- Inertial weight= 0.4;
- Alpha= 0.4;
- Beta= 0.4;
- C1= 2.0;
- C2= 2.0;
- Random seed= 26;
- No-WAIM case implemented by the first particle at the 1st iteration;
- Samples synthesis (phi cuts): $\theta \in [0, 90] [deg]$, $\varphi \in [0, 90] [deg]$, $\theta_{samples} = 7$, $\varphi_{samples} = 3$;

Optimization Results

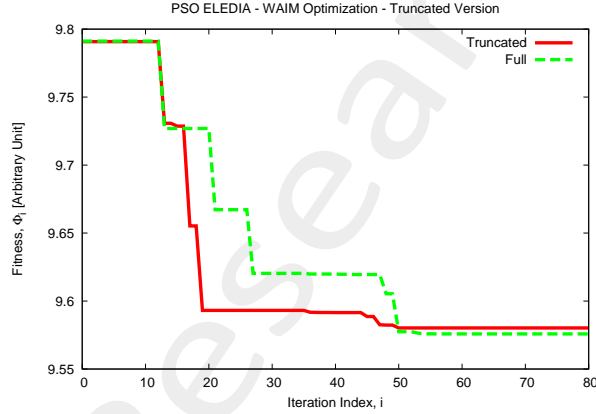


Figure 2: Fitness Dynamics.

Simulation time (Truncated) : 298m 42s

Simulation time (Full) : 1132m 38s

We ran the optimization using both the full and the truncated version of the software, with the same parameters, in order to identify some possible differences, but the simulations ended up with almost the same results.

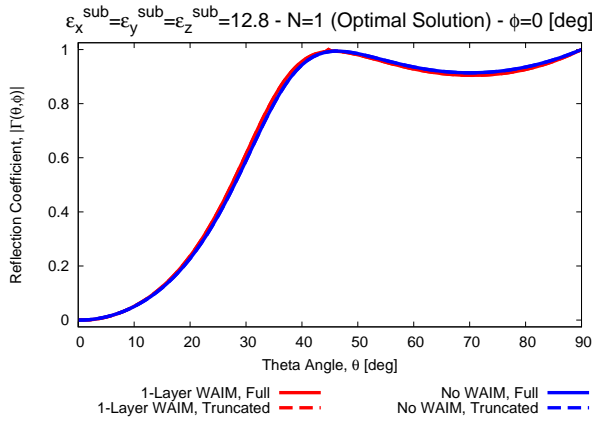
| <i>Tool</i> | <i>Optimal Solution</i> | | <i>Fitness Value</i> | |
|------------------|---|-----------------|----------------------|---------------|
| | $\varepsilon_x^1 = \varepsilon_y^1 = \varepsilon_z^1$ | $h^1 [\lambda]$ | $\Phi_{i=0}$ | $\Phi_{I=80}$ |
| <i>Truncated</i> | 1.0154 | 0.5 | 9.791 | 9.580 |
| <i>Full</i> | 1.0153 | 0.5 | 9.791 | 9.576 |

Table 1: Optimal Solutions.

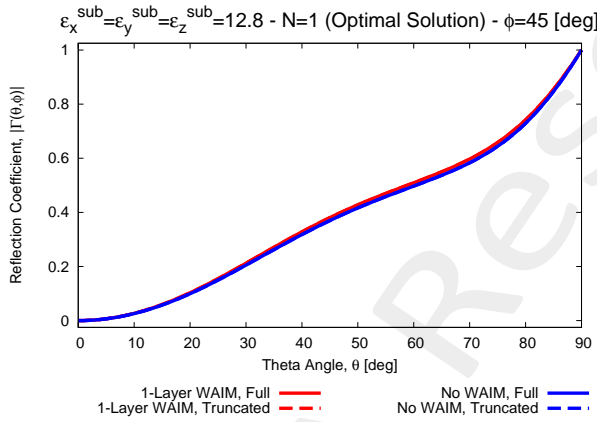
Even if the "Full" simulation has a lower Fitness value, the difference with respect to the "Truncated" case is very tiny, compared with the difference in computational time. Therefore, for the next simulations we will run only the "Truncated" version.

This first simulation takes as example the one performed, but considers different ranges. In particular, the most important difference is on the ε^1 range: is set as $[-5 : 5]$. This allowed to explore solution with ε^1 lower than 1 (Free Space), and even negative solutions.

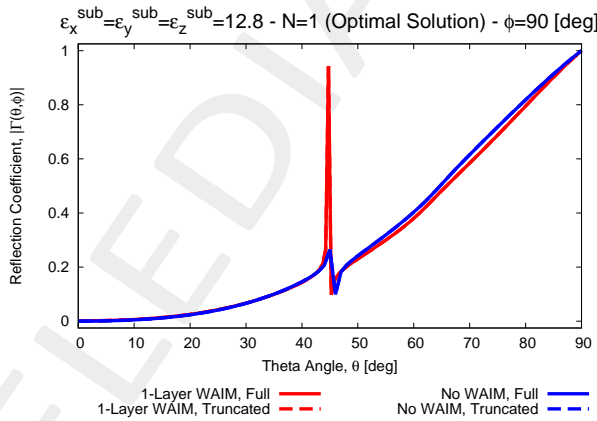
Our case, instead, takes as borderline case the Free Space solution ($\varepsilon^1 = [1 : 5]$). Indeed, as reported in the previous table (Table 1 on page 4), we can notice that the optimal solution has a value of ε^1 very close to 1.



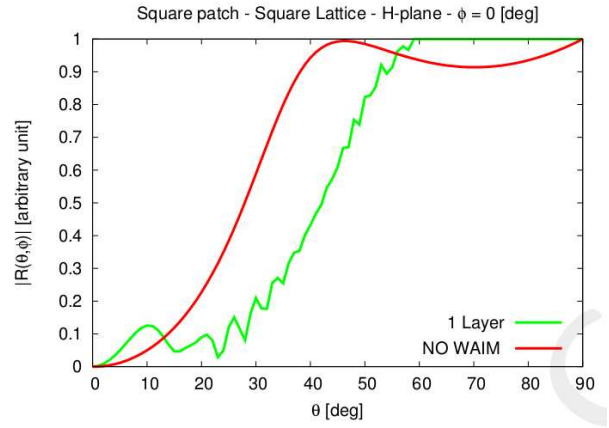
(a) $\varphi = 0[deg]$



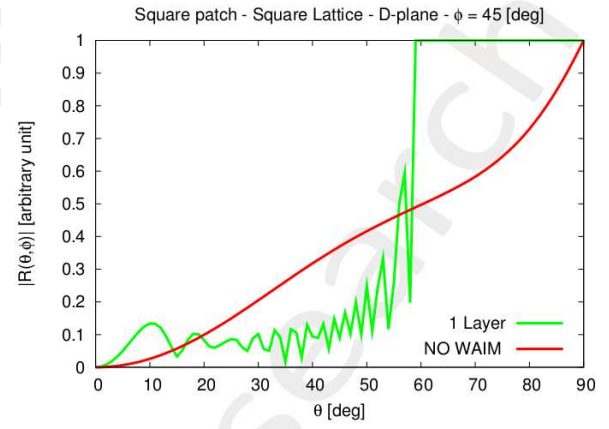
(c) $\varphi = 45[deg]$



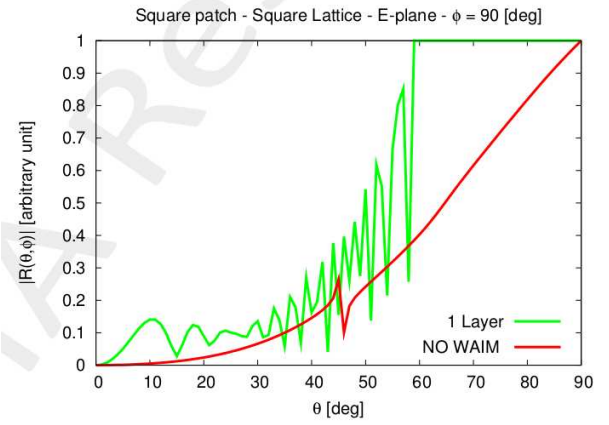
(e) $\varphi = 90[deg]$



(b) $\varphi = 0[deg]$, from reference report



(d) $\varphi = 45[deg]$, from reference report



(f) $\varphi = 90[deg]$, from reference report

Figure 3: Reflection Coefficient along φ cuts, 1 Layer WAIM.

The higher peak in Figure 3 on page 5(e) is probably due to a more dense sampling along θ .

From the images, we can notice that our solution is almost identical to the non-covered case, but it slightly reduces the Reflection Coefficient Γ for values of $\theta > 80[deg]$. On the contrary, the solution proposed has an high non linear behaviour and a total reflection for $\theta > 60[deg]$.

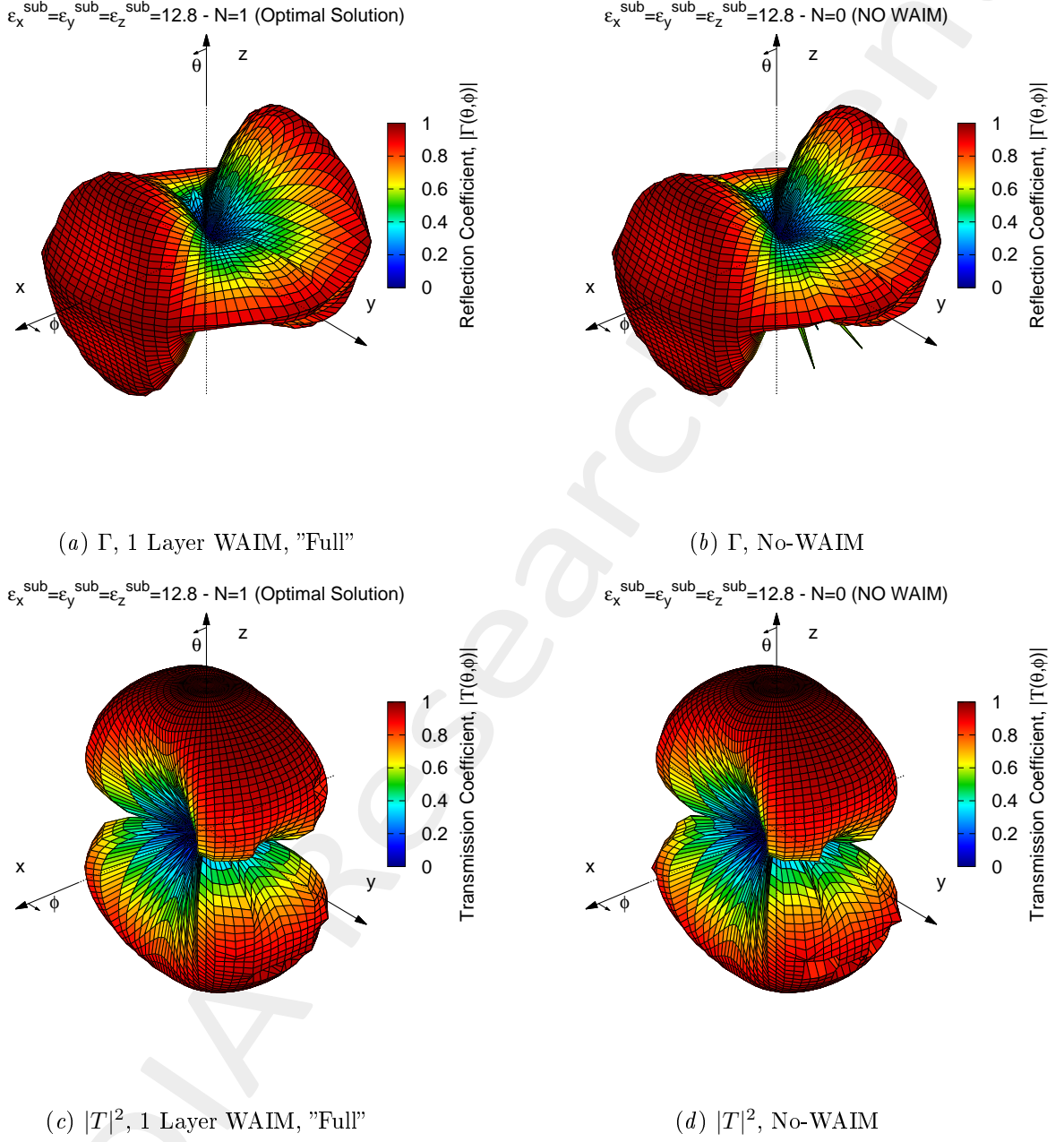


Figure 4: Reflection Coefficient and Transmission Coefficient

| Tool | Cost Function | | Improvement Percentage |
|-----------|-----------------|---------------------|------------------------|
| | Φ_0^{fine} | Φ_{SbD}^{fine} | |
| Full | 663.46 | 661.75 | -0.26% |
| Truncated | 663.51 | 661.72 | -0.27% |

Table 2: Cost Function Improvement.

1.1.2 Test Case #2 - Single Frequency - 1 Isotropic WAIM Layer - $\epsilon^1 = [1 : 35] + j0$ - Square Lattice - $\epsilon^{sub} = 12.8$ Tests

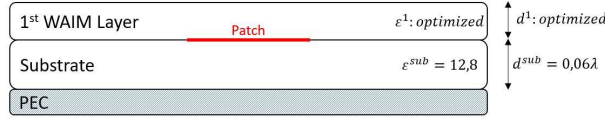


Figure 5: Test Case Schema.

Simulation Parameters:

- Frequency: $f = 10[GHz]$;
- Patch dimensions: $w = 0.15, l = 0.098 [\lambda]$;
- Probe position: $x = 0.049, y = 0.0 [\lambda]$;
- Substrate: $\epsilon_x = 12.8 + j0, \epsilon_y = 12.8 + j0, \epsilon_z = 12.8 + j0, d = 0.06[\lambda]$
- Floquet coefficient = 121;
- Lattice basis: $s_1 = (0.5, 0.0), s_2 = (0.0, 0.5) [\lambda]$;

Analysis Parameters:

- Samples analysis (phi cuts): $\theta \in [0, 90] [deg], \varphi \in [0, 90] [deg], \theta_{samples} = 182, \varphi_{samples} = 3$;
- Samples analysis (3D plots): $\theta \in [-180, 180] [deg], \varphi \in [-90, 90] [deg], \theta_{samples} = 72, \varphi_{samples} = 21$;

PSO Synthesis Parameters:

- Number of WAIM Layers: $N = 1$;
- Unknowns: $U = 2$;
- Unknown ranges: $\epsilon = [1 : 35] + j0, d = [0.033 : 0.5] [\lambda]$;
- Swarm size: $P = 6$;
- Max iteration number: $I = 80$;
- Inertial weight= 0.4;
- Alpha= 0.4;
- Beta= 0.4;
- C1= 2.0;
- C2= 2.0;

- Random seed= 26;
- No-WAIM case implemented by the first particle at the 1st iteration;
- Samples synthesis (phi cuts): $\theta \in [0, 90]$ [deg], $\varphi \in [0, 90]$ [deg], $\theta_{samples} = 7$, $\varphi_{samples} = 3$;

Optimization Results

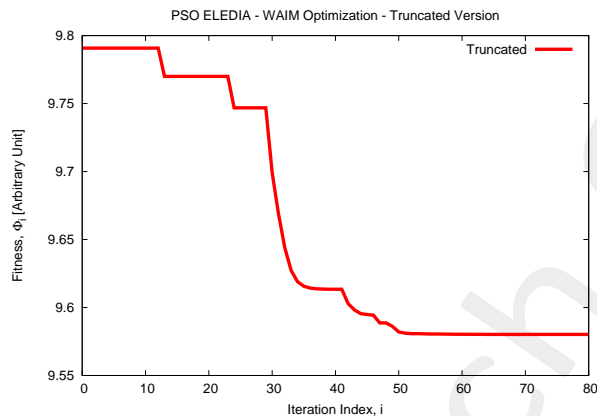


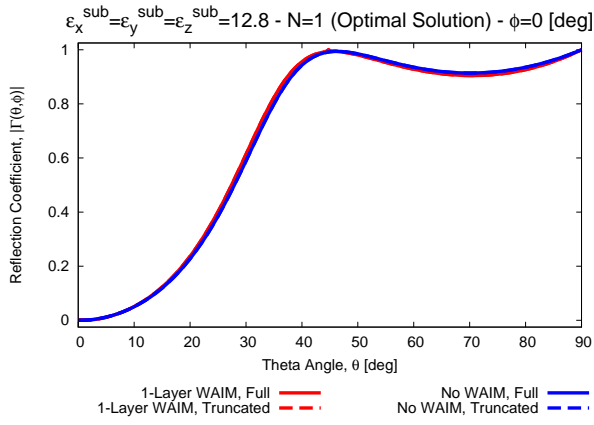
Figure 6: Fitness Dynamics.

Simulation time (Truncated) : 299m 01s

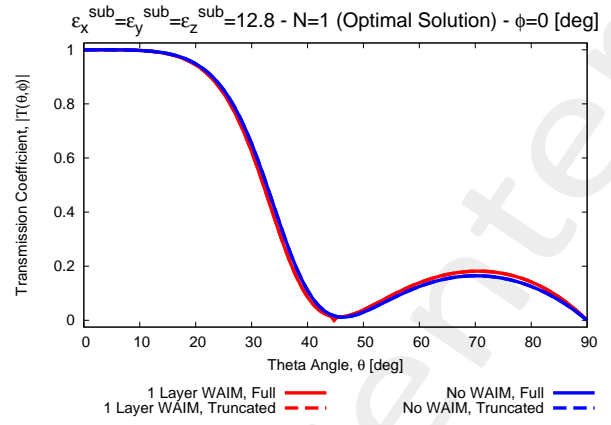
Since the results obtained in 1.1.1 are very similar to the ones obtained for the Non-Covered case, in this simulation we enlarged the solution space by setting $\varepsilon^1 = [1 : 35]$.

| <i>Tool</i> | <i>Optimal Solution</i> | | <i>Fitness Value</i> | |
|------------------|---|-----------------|----------------------|---------------|
| | $\varepsilon_x^1 = \varepsilon_y^1 = \varepsilon_z^1$ | $h^1 [\lambda]$ | $\Phi_{i=0}$ | $\Phi_{I=80}$ |
| <i>Truncated</i> | 1.015 | 0.5 | 9.791 | 9.580 |

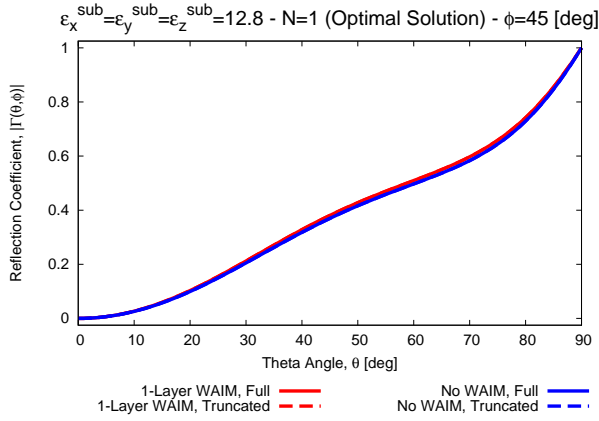
Table 3: Optimal Solution.



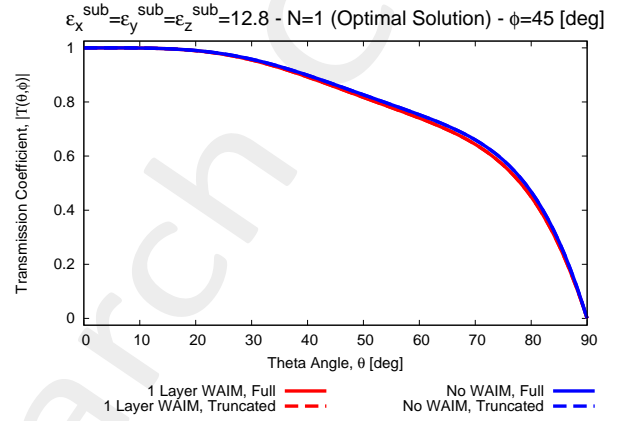
(a) Γ , $\varphi = 0$ [deg]



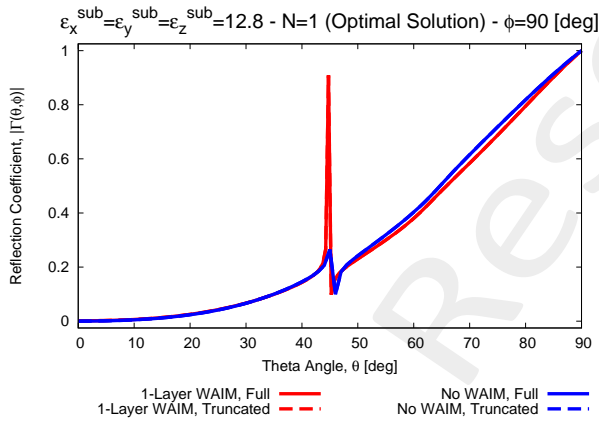
(b) $|T|^2$, $\varphi = 0$ [deg]



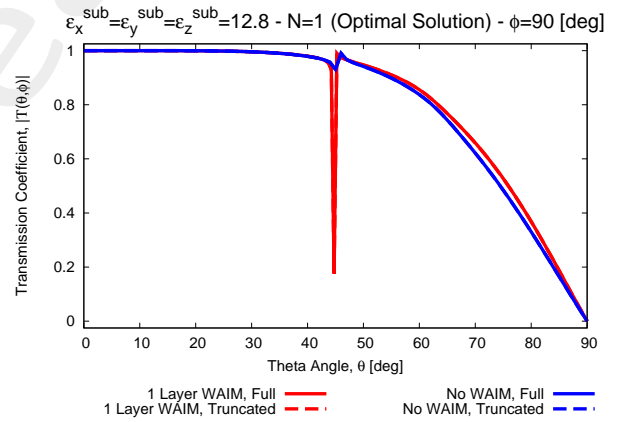
(c) Γ , $\varphi = 45$ [deg]



(d) $|T|^2$, $\varphi = 45$ [deg]



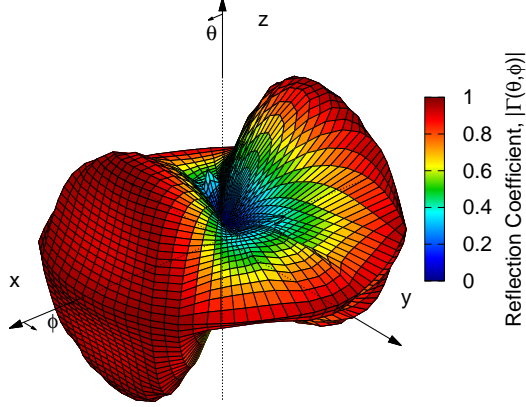
(e) Γ , $\varphi = 90$ [deg]



(f) $|T|^2$, $\varphi = 90$ [deg]

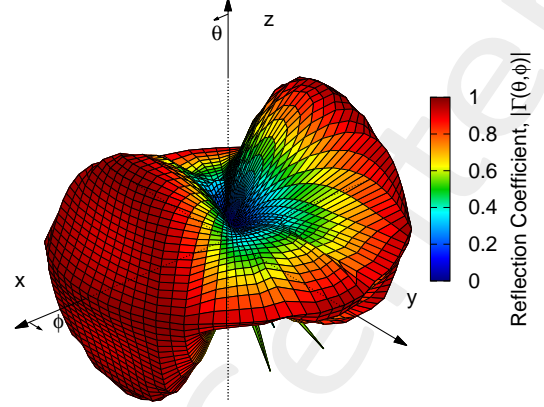
Figure 7: Reflection Coefficient along φ cuts, 1 Layer WAIM.

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=1$ (Optimal Solution)



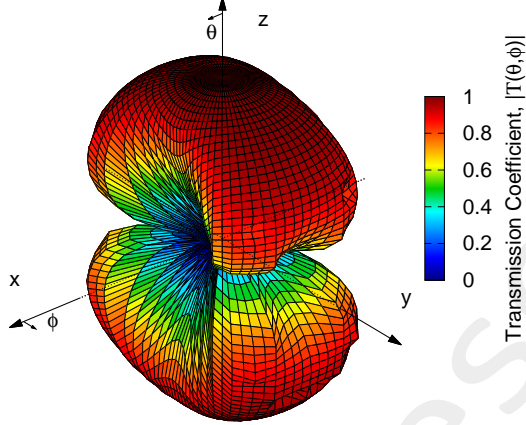
(a) Γ , 1 Layer WAIM, "Full"

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=0$ (NO WAIM)



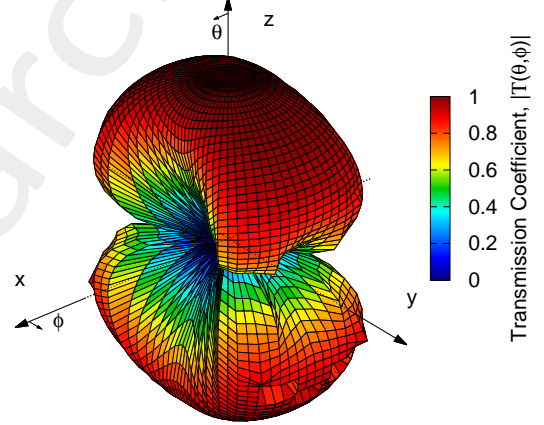
(b) Γ , No-WAIM

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=1$ (Optimal Solution)



(c) $|T|^2$, 1 Layer WAIM, "Full"

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=0$ (NO WAIM)



(d) $|T|^2$, No-WAIM

Figure 8: Reflection Coefficient and Transmission Coefficient

As we can notice, the obtained value are still very close to the No-WAIM case. Moreover, increasing the maximum value of ϵ^1 has not lead to any improvement, since the optimal solution still tends to the Free Space.

| Tool | Cost Function | | Improvement Percentage |
|-----------|------------------------|-----------------------------------|------------------------|
| | Φ_0^{fine} | $\Phi_{\text{ShD}}^{\text{fine}}$ | |
| Full | 663.46 | 661.78 | -0.25% |
| Truncated | 663.51 | 661.75 | -0.26% |

Table 4: Cost Function Improvement.

1.1.3 Test Case #3 - Single Frequency - 1 Anisotropic WAIM Layer - $\epsilon^1 = [1 : 35] + j0$ - Square Lattice - $\epsilon^{sub} = 12.8$ Tests

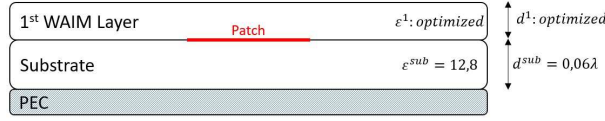


Figure 9: Test Case Schema.

Simulation Parameters:

- Frequency: $f = 10[GHz]$;
- Patch dimensions: $w = 0.15, l = 0.098 [\lambda]$;
- Probe position: $x = 0.049, y = 0.0 [\lambda]$;
- Substrate: $\epsilon_x = 12.8 + j0, \epsilon_y = 12.8 + j0, \epsilon_z = 12.8 + j0, d = 0.06[\lambda]$
- Floquet coefficient = 121;
- Lattice basis: $s_1 = (0.5, 0.0), s_2 = (0.0, 0.5) [\lambda]$;

Analysis Parameters:

- Samples analysis (phi cuts): $\theta \in [0, 90] [deg], \varphi \in [0, 90] [deg], \theta_{samples} = 182, \varphi_{samples} = 3$;
- Samples analysis (3D plots): $\theta \in [-180, 180] [deg], \varphi \in [-90, 90] [deg], \theta_{samples} = 72, \varphi_{samples} = 21$;

PSO Synthesis Parameters:

- Number of WAIM Layers: $N = 1$;
- Unknowns: $U = 4$;
- Unknown ranges: $\epsilon_{xx} = [1 : 35] + j0, \epsilon_{yy} = [1 : 35] + j0, \epsilon_{zz} = [1 : 35] + j0, d = [0.033 : 0.5] [\lambda]$;
- Swarm size: $P = 6$;
- Max iteration number: $I = 80$;
- Inertial weight= 0.4;
- Alpha= 0.4;
- Beta= 0.4;
- C1= 2.0;
- C2= 2.0;

- Random seed= 26;
- No-WAIM case implemented by the first particle at the 1st iteration;
- Samples synthesis (phi cuts): $\theta \in [0, 90]$ [deg], $\varphi \in [0, 90]$ [deg], $\theta_{samples} = 7$, $\varphi_{samples} = 3$;

Optimization Results

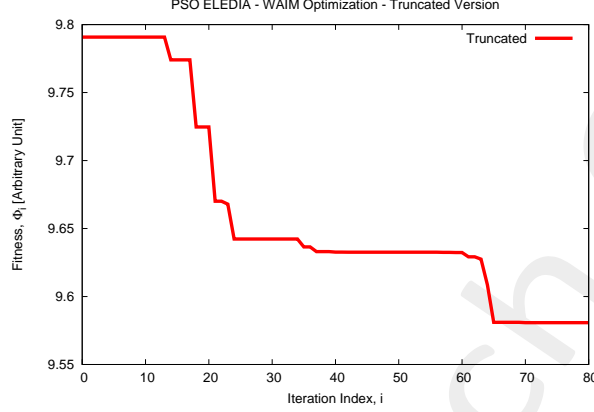


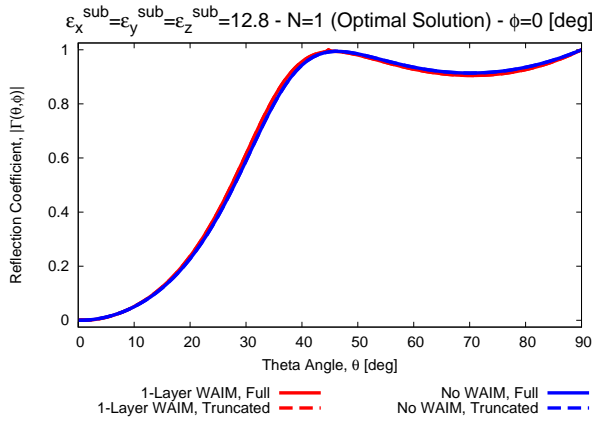
Figure 10: Fitness Dynamics.

Simulation time (Truncated) : 298m 51s

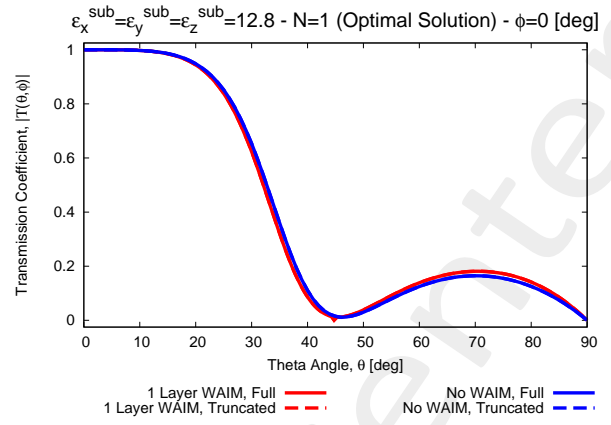
From the previous tests, we have seen that dealing with Isotropic materials does not lead the big improvements in the radiation performance of the array. Indeed, even if we set ranges of ε^1 with an high maximum value, the optimal solution will tend to Free Space values. Thus, in this simulation, we will consider Anisotropic materials. All the ε components (ε_x^1 , ε_y^1 and ε_z^1) have the same range ($[1 : 35] + j0$), but their value will be optimized singularly, as independent variables.

| <i>Tool</i> | <i>Optimal Solution</i> | | | | <i>Fitness Value</i> | |
|------------------|-------------------------|-------------------|-------------------|---------------------|----------------------|---------------|
| | ε_x^1 | ε_y^1 | ε_z^1 | h^1 [λ] | $\Phi_{i=0}$ | $\Phi_{I=80}$ |
| <i>Truncated</i> | 1.015 | 8.904 | 1.376 | 0.49 | 9.791 | 9.581 |

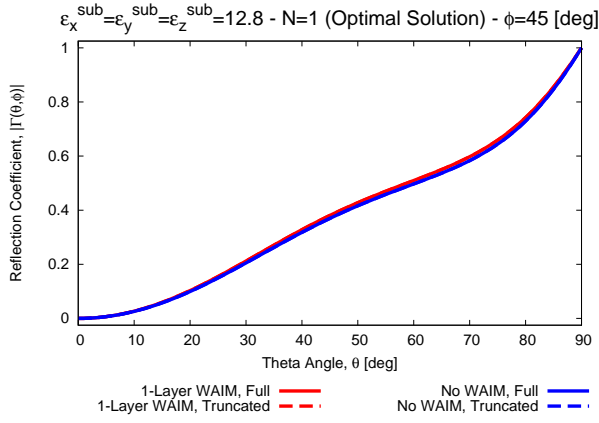
Table 5: Optimal Solution.



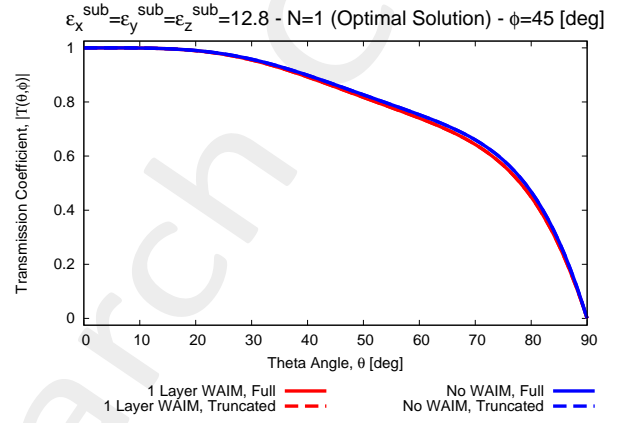
(a) Γ , $\varphi = 0$ [deg]



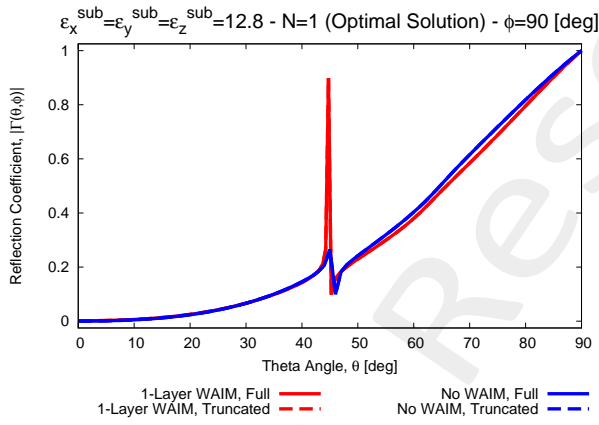
(b) $|T|^2$, $\varphi = 0$ [deg]



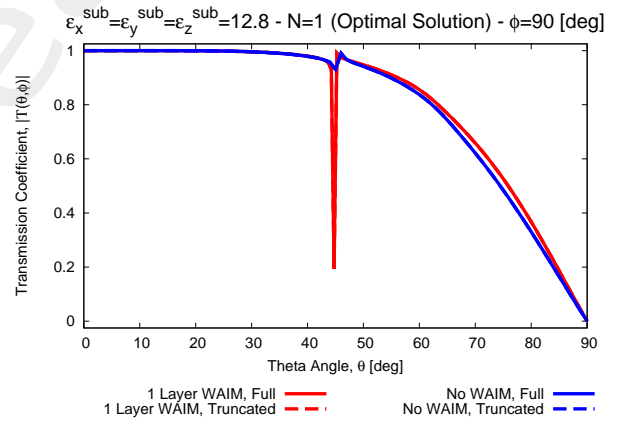
(c) Γ , $\varphi = 45$ [deg]



(d) $|T|^2$, $\varphi = 45$ [deg]



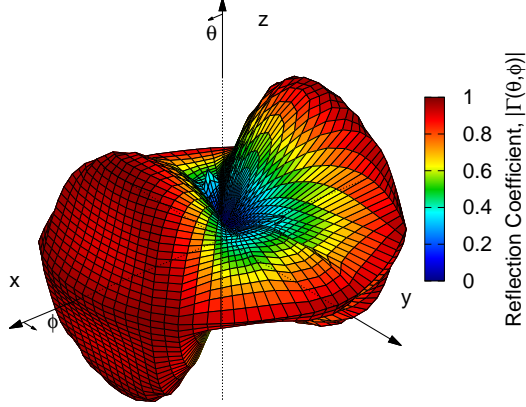
(e) Γ , $\varphi = 90$ [deg]



(f) $|T|^2$, $\varphi = 90$ [deg]

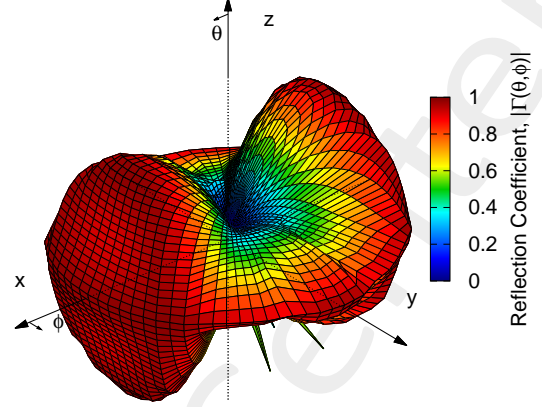
Figure 11: Reflection Coefficient along φ cuts, 1 Layer WAIM.

$\varepsilon_x^{\text{sub}} = \varepsilon_y^{\text{sub}} = \varepsilon_z^{\text{sub}} = 12.8 - N=1$ (Optimal Solution)



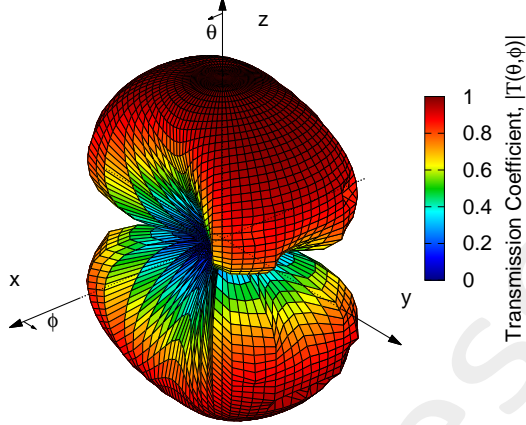
(a) Γ , 1 Layer WAIM, "Full"

$\varepsilon_x^{\text{sub}} = \varepsilon_y^{\text{sub}} = \varepsilon_z^{\text{sub}} = 12.8 - N=0$ (NO WAIM)



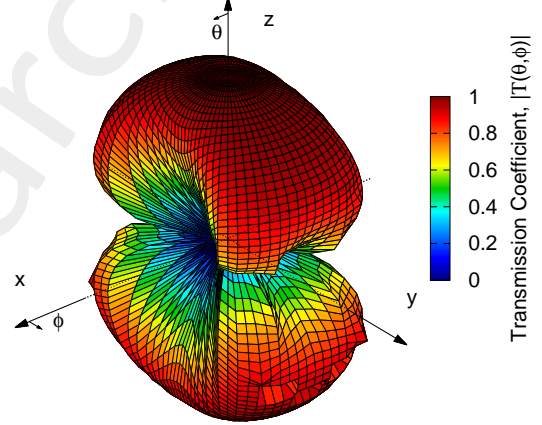
(b) Γ , No-WAIM

$\varepsilon_x^{\text{sub}} = \varepsilon_y^{\text{sub}} = \varepsilon_z^{\text{sub}} = 12.8 - N=1$ (Optimal Solution)



(c) $|T|^2$, 1 Layer WAIM, "Full"

$\varepsilon_x^{\text{sub}} = \varepsilon_y^{\text{sub}} = \varepsilon_z^{\text{sub}} = 12.8 - N=0$ (NO WAIM)



(d) $|T|^2$, No-WAIM

Figure 12: Reflection Coefficient and Transmission Coefficient

| Tool | Cost Function | | Improvement Percentage |
|-----------|------------------------|-----------------------------------|------------------------|
| | Φ_0^{fine} | $\Phi_{\text{SbD}}^{\text{fine}}$ | |
| Full | 663.46 | 661.78 | -0.25% |
| Truncated | 663.51 | 661.75 | -0.26% |

Table 6: Cost Function Improvement.

As we can notice from Table 5 on page 12, the values of ε_x^1 , ε_z^1 and d^1 and *Fitness* are almost unchanged with respect to the ones obtained in 1.1.2. Instead, the value of ε_y^1 is pretty high. However, the performance obtained are still similar to the Non-Covered case. Therefore, we could infer that it is not possible to improve the radiation performance only by acting on the real part of ε^1 of a single layer. Moreover, some doubts could arise on the effective utility of an Anisotropic material.

1.1.4 Test Case #4 - Single Frequency - 1 Isotropic WAIM Layer - $\epsilon^1 = [1 : 35] + j[0 : 35]$ - Square Lattice - $\epsilon^{sub} = 12.8$ Tests

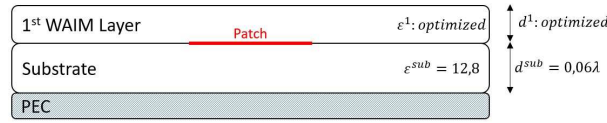


Figure 13: Test Case Schema.

Simulation Parameters:

- Frequency: $f = 10[GHz]$;
- Patch dimensions: $w = 0.15, l = 0.098 [\lambda]$;
- Probe position: $x = 0.049, y = 0.0 [\lambda]$;
- Substrate: $\epsilon_x = 12.8 + j0, \epsilon_y = 12.8 + j0, \epsilon_z = 12.8 + j0, d = 0.06[\lambda]$
- Floquet coefficient = 121;
- Lattice basis: $s_1 = (0.5, 0.0), s_2 = (0.0, 0.5) [\lambda]$;

Analysis Parameters:

- Samples analysis (phi cuts): $\theta \in [0, 90] [deg], \varphi \in [0, 90] [deg], \theta_{samples} = 182, \varphi_{samples} = 3$;
- Samples analysis (3D plots): $\theta \in [-180, 180] [deg], \varphi \in [-90, 90] [deg], \theta_{samples} = 72, \varphi_{samples} = 21$;

PSO Synthesis Parameters:

- Number of WAIM Layers: $N = 1$;
- Unknowns: $U = 3$;
- Unknown ranges: $\epsilon = [1 : 35] + j[0 : 35], d = [0.033 : 0.5] [\lambda]$;
- Swarm size: $P = 6$;
- Max iteration number: $I = 80$;
- Inertial weight= 0.4;
- Alpha= 0.4;
- Beta= 0.4;
- C1= 2.0;
- C2= 2.0;

- Random seed= 26;
- No-WAIM case implemented by the first particle at the 1st iteration;
- Samples synthesis (phi cuts): $\theta \in [0, 90] [deg]$, $\varphi \in [0, 90] [deg]$, $\theta_{samples} = 7$, $\varphi_{samples} = 3$;

Optimization Results

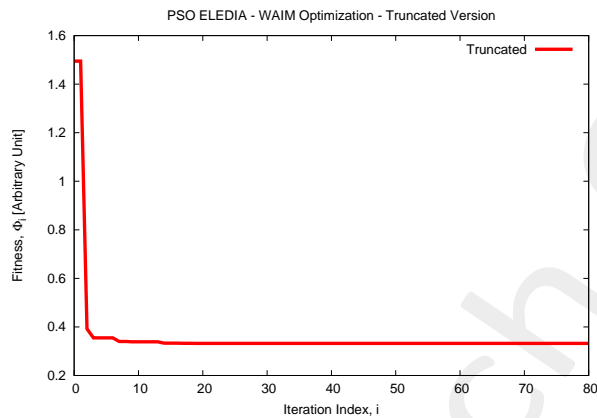
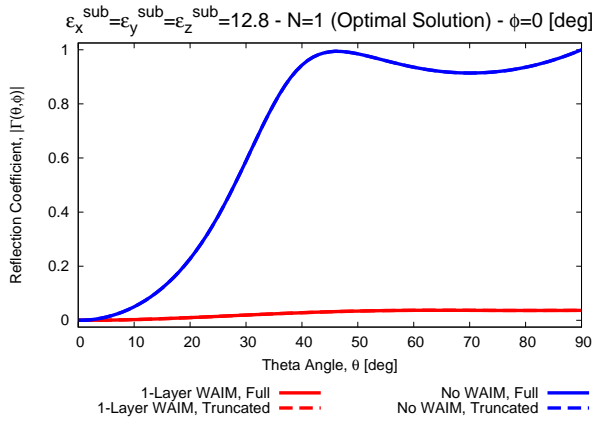


Figure 14: Fitness Dynamics.

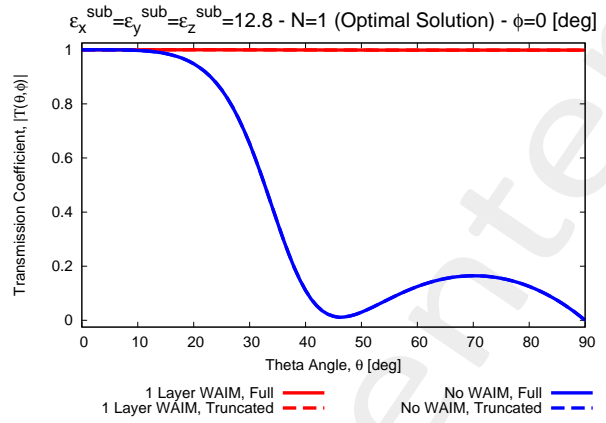
Simulation time (Truncated) : 302m 10s

| <i>Tool</i> | <i>Optimal Solution</i> | | | <i>Fitness Value</i> | |
|------------------|---|---|-----------------|----------------------|---------------|
| | $Re\{\varepsilon_x^1\} = Re\{\varepsilon_y^1\} = Re\{\varepsilon_z^1\}$ | $Im\{\varepsilon_x^1\} = Im\{\varepsilon_y^1\} = Im\{\varepsilon_z^1\}$ | $h^1 [\lambda]$ | $\Phi_{i=0}$ | $\Phi_{I=80}$ |
| <i>Truncated</i> | 1.0 | 5.79 | 0.23 | 1.495 | 0.332 |

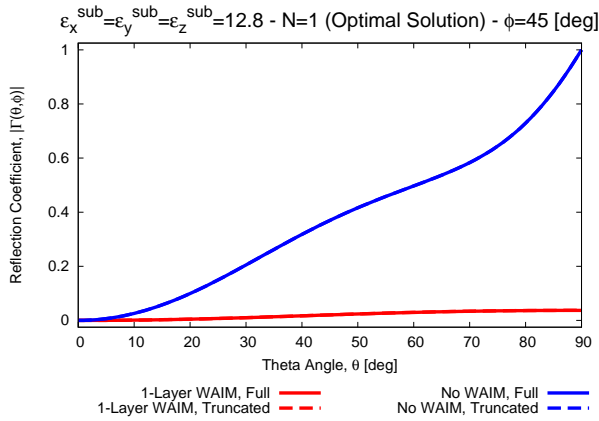
Table 7: Optimal Solution.



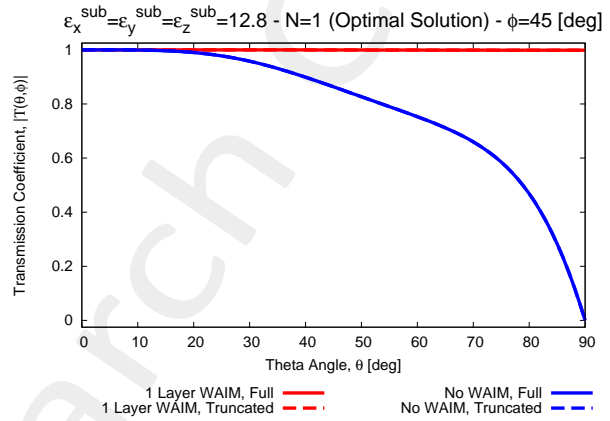
(a) Γ , $\varphi = 0$ [deg]



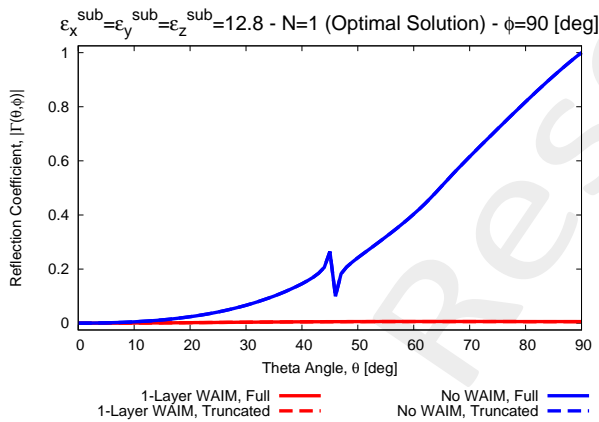
(b) $|T|^2$, $\varphi = 0$ [deg]



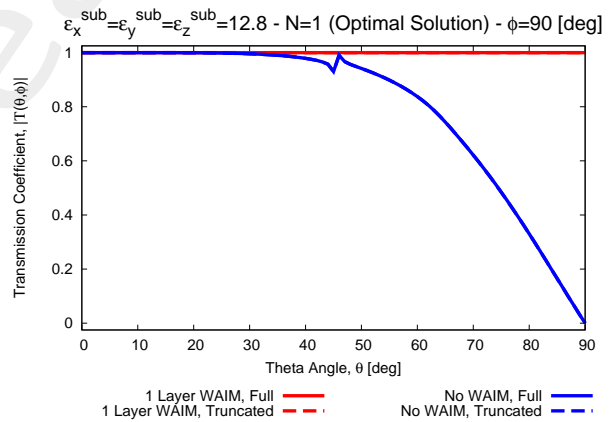
(c) Γ , $\varphi = 45$ [deg]



(d) $|T|^2$, $\varphi = 45$ [deg]



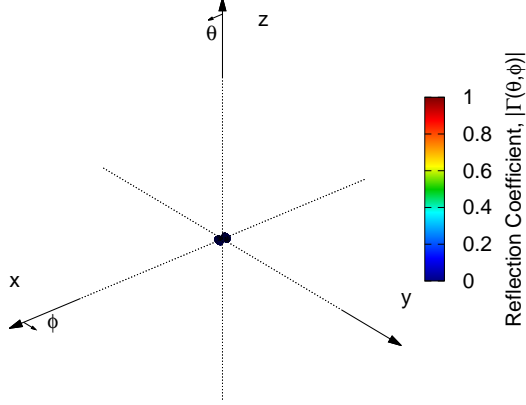
(e) Γ , $\varphi = 90$ [deg]



(f) $|T|^2$, $\varphi = 90$ [deg]

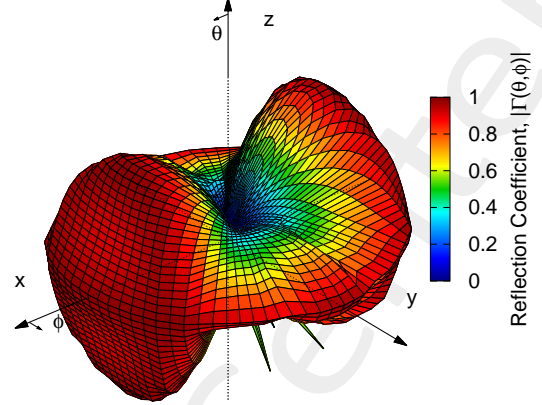
Figure 15: Reflection Coefficient along φ cuts, 1 Layer WAIM.

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=1$ (Optimal Solution)



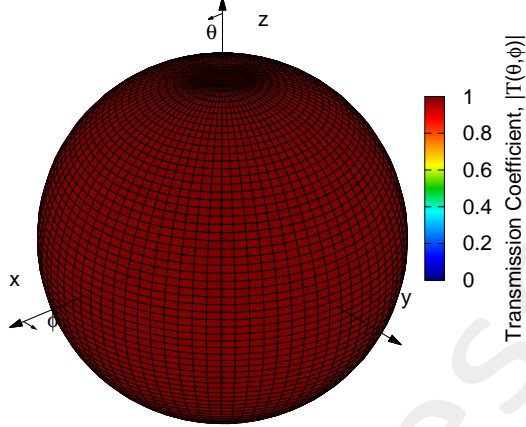
(a) Γ , 1 Layer WAIM, "Full"

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=0$ (NO WAIM)



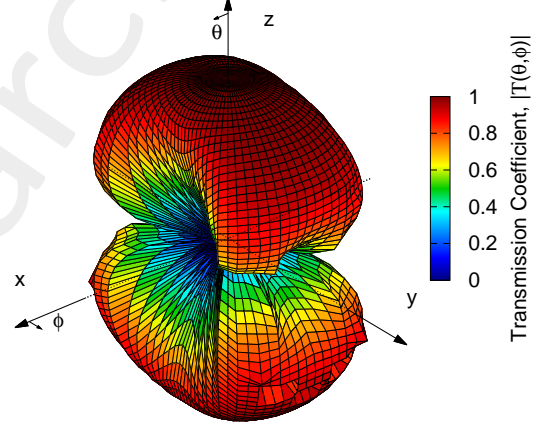
(b) Γ , No-WAIM

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=1$ (Optimal Solution)



(c) $|T|^2$, 1 Layer WAIM, "Full"

$\epsilon_x^{\text{sub}} = \epsilon_y^{\text{sub}} = \epsilon_z^{\text{sub}} = 12.8 - N=0$ (NO WAIM)



(d) $|T|^2$, No-WAIM

Figure 16: Reflection Coefficient and Transmission Coefficient

| Tool | Cost Function | | Improvement Percentage |
|-----------|------------------------|-----------------------------------|------------------------|
| | Φ_0^{fine} | $\Phi_{\text{SbD}}^{\text{fine}}$ | |
| Full | 663.46 | 23.24 | -96.50% |
| Truncated | 663.51 | 23.33 | -96.48% |

Table 8: Cost Function Improvement.

Acting on the $\text{Im}\{\epsilon^1\}$, finally, we are able to almost perfectly match the impedance, leading to a an excellent radiation pattern along all the possible steering directions (θ, ϕ) .

More information on the topics of this document can be found in the following list of references.

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