

# Multi-Scaling Bayesian Compressive Sensing Imaging of Dielectric Objects

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## Abstract

In this work, a new Bayesian compressive sensing (*BCS*)-based imaging technique is proposed to exploit additional information besides that on the target *sparsity*. More precisely, an innovative iterative multi-scaling (*IMSA*)-*BCS* scheme is proposed to combine the a-priori knowledge on the class of scatterers and the progressively acquired information on the location and the size of the unknown object. Accordingly the 2D transverse magnetic (*TM*) inverse scattering problem is solved by means of an innovative *IMSA*-based information-driven relevance vector machine (*RVM*) solver. Some numerical results are shown to verify the effectiveness of the proposed imaging technique.

# 1 Numerical Assessment

## 1.1 L-shaped Object, $\ell = 1.5\lambda$

### Test Case Description

#### Direct solver:

- Side of the investigation domain:  $L = 6.0\lambda$
- Cubic domain divided in  $\sqrt{D} \times \sqrt{D}$  cells
- Number of cells for the direct solver:  $D = 1600$  (discretization =  $\lambda/10$ )

#### Investigation domain:

- Cubic domain divided in  $\sqrt{N} \times \sqrt{N}$  cells
- Number of cells for the inversion:
  - First Step IMSA:  $N^{(1)} = 100$  (discretization =  $\lambda/10$ )
  - Following Steps IMSA:  $N^{(i)}$  not fixed, defined according to the estimated  $RoI \mathcal{D}^{(i)}$

#### Measurement domain:

- Total number of measurements:  $M = 60$
- Measurement points placed on circles of radius  $\rho = 4.5\lambda$

#### Sources:

- Plane waves
- Number of views:  $V = 60$ ;  $\theta_{inc}^v = 0^\circ + (v - 1) \times (360/V)$
- Amplitude:  $A = 1.0$
- Frequency:  $F = 300$  MHz ( $\lambda = 1$ )

#### Background:

- $\varepsilon_r = 1.0$
- $\sigma = 0$  [S/m]

#### Scatterer

- L-shaped object,  $\ell = 1.5\lambda$
- $\varepsilon_r \in \{1.01, 1.02, 1.04, 1.05, 1.06, 1.08, 1.10, 1.15, 1.20\}$
- $\sigma = 0$  [S/m]

1.1.1 L-shaped Object,  $\ell = 1.5\lambda$ ,  $\tau = 0.02$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

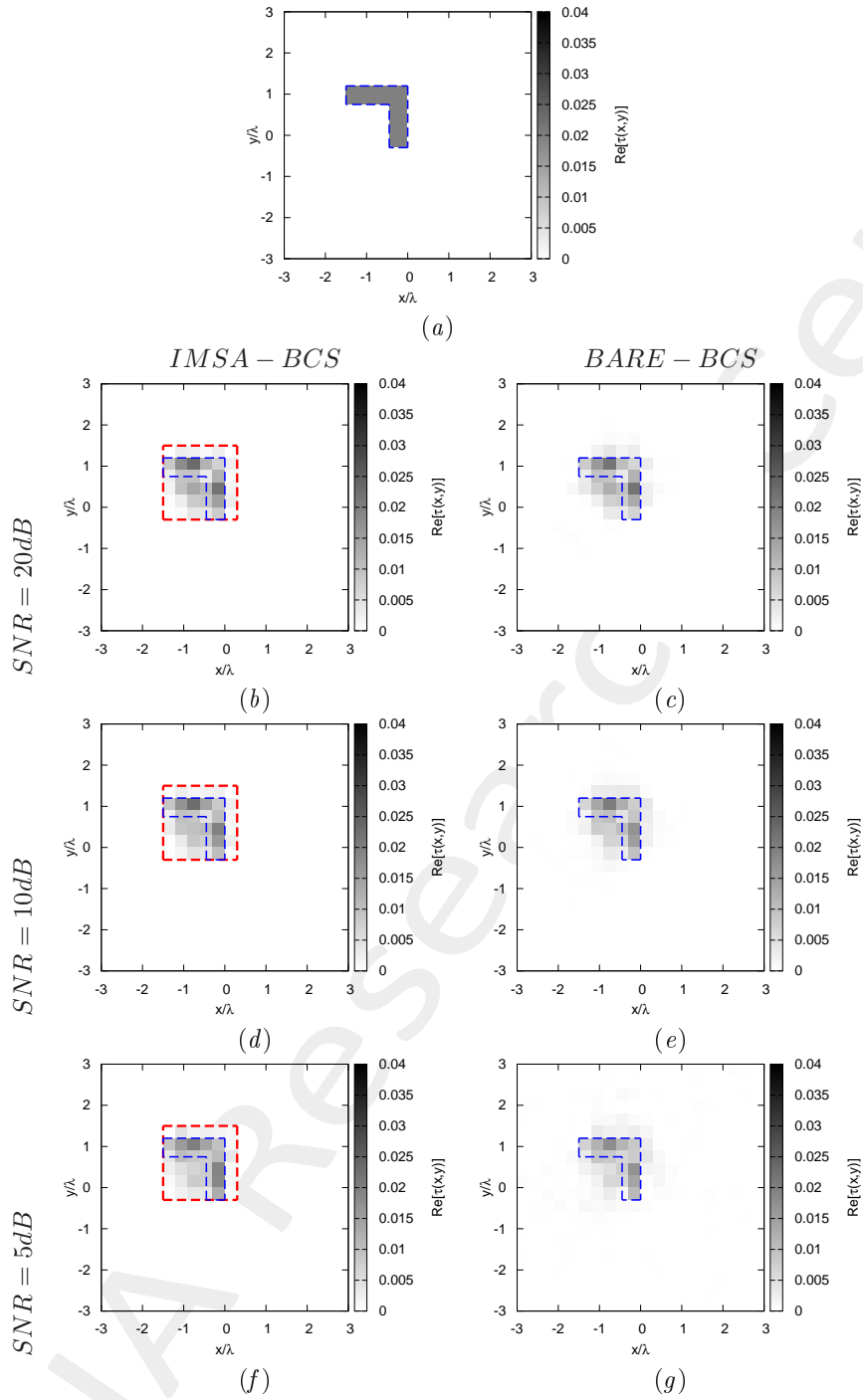


Figure 1: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\ell = 1.5\lambda$ ,  $\tau = 0.02$  - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].

<i>SNR = 50dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$5.64 \times 10^{-4}$	$5.15 \times 10^{-4}$
$\xi_{int}$	$1.04 \times 10^{-2}$	$9.08 \times 10^{-3}$
$\xi_{ext}$	$2.39 \times 10^{-4}$	$2.32 \times 10^{-4}$
<i>SNR = 20dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$5.72 \times 10^{-4}$	$5.26 \times 10^{-4}$
$\xi_{int}$	$1.04 \times 10^{-2}$	$9.26 \times 10^{-3}$
$\xi_{ext}$	$2.47 \times 10^{-4}$	$2.37 \times 10^{-4}$
<i>SNR = 10dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$5.42 \times 10^{-4}$	$5.36 \times 10^{-4}$
$\xi_{int}$	$1.01 \times 10^{-2}$	$9.17 \times 10^{-3}$
$\xi_{ext}$	$2.24 \times 10^{-4}$	$2.49 \times 10^{-4}$
<i>SNR = 5dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$4.34 \times 10^{-4}$	$6.03 \times 10^{-4}$
$\xi_{int}$	$7.44 \times 10^{-3}$	$9.57 \times 10^{-3}$
$\xi_{ext}$	$2.01 \times 10^{-4}$	$2.85 \times 10^{-4}$

Table I: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.02$  - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.

1.1.2 L-shaped Object,  $\ell = 1.5\lambda$ ,  $\tau = 0.05$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

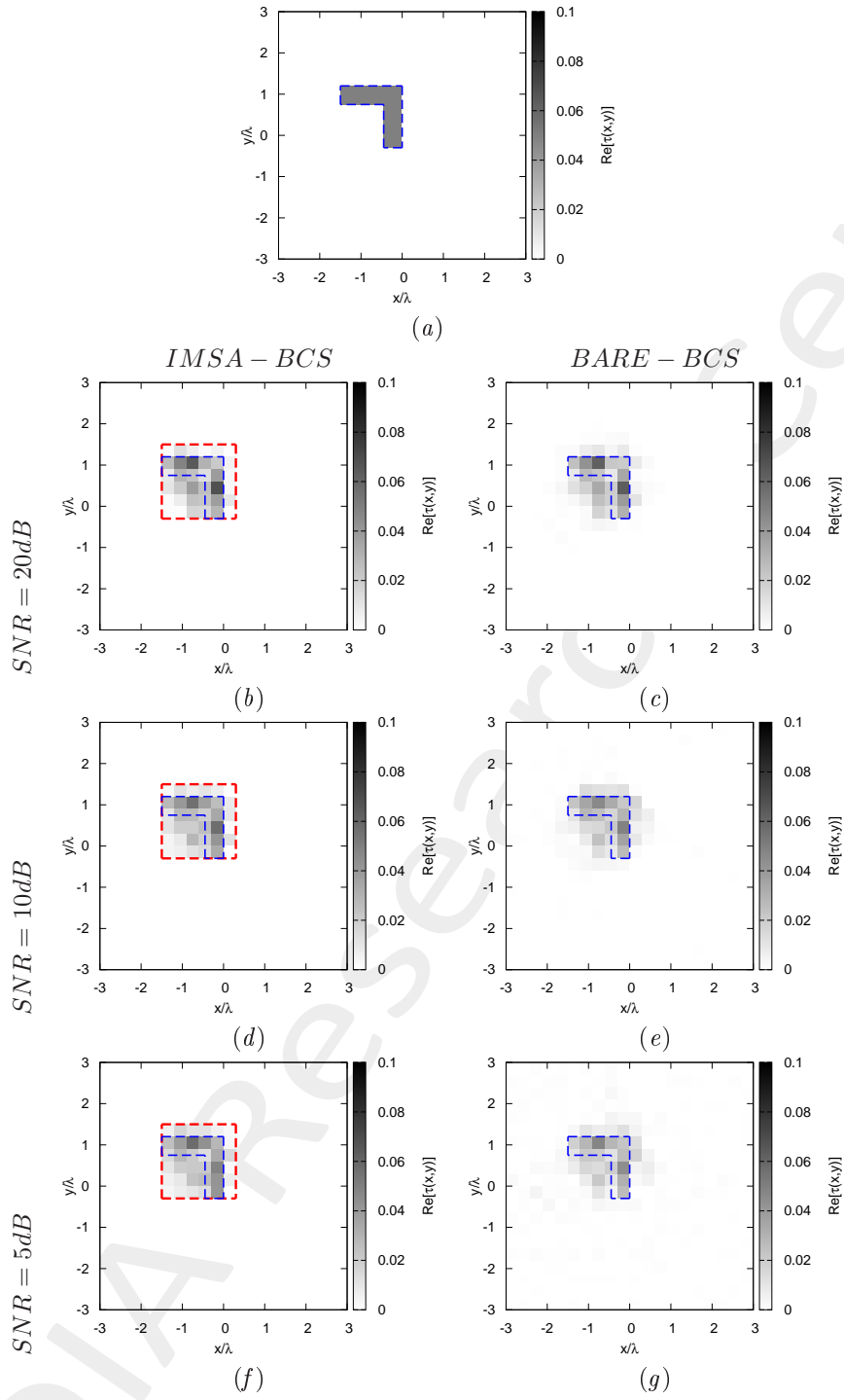


Figure 2: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.05$  - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].

<i>SNR = 50dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$1.23 \times 10^{-3}$	$1.31 \times 10^{-3}$
$\xi_{int}$	$1.99 \times 10^{-2}$	$2.00 \times 10^{-2}$
$\xi_{ext}$	$6.12 \times 10^{-4}$	$6.78 \times 10^{-4}$
<i>SNR = 20dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$1.23 \times 10^{-3}$	$1.39 \times 10^{-3}$
$\xi_{int}$	$1.98 \times 10^{-2}$	$2.14 \times 10^{-2}$
$\xi_{ext}$	$6.17 \times 10^{-4}$	$7.21 \times 10^{-4}$
<i>SNR = 10dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$1.19 \times 10^{-3}$	$1.57 \times 10^{-3}$
$\xi_{int}$	$1.74 \times 10^{-2}$	$2.01 \times 10^{-2}$
$\xi_{ext}$	$6.50 \times 10^{-4}$	$8.84 \times 10^{-4}$
<i>SNR = 5dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$1.19 \times 10^{-3}$	$1.98 \times 10^{-3}$
$\xi_{int}$	$1.66 \times 10^{-2}$	$2.31 \times 10^{-2}$
$\xi_{ext}$	$6.73 \times 10^{-4}$	$1.09 \times 10^{-3}$

Table II: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.05$  - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.

1.1.3 L-shaped Object,  $\ell = 1.5\lambda$ ,  $\tau = 0.10$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

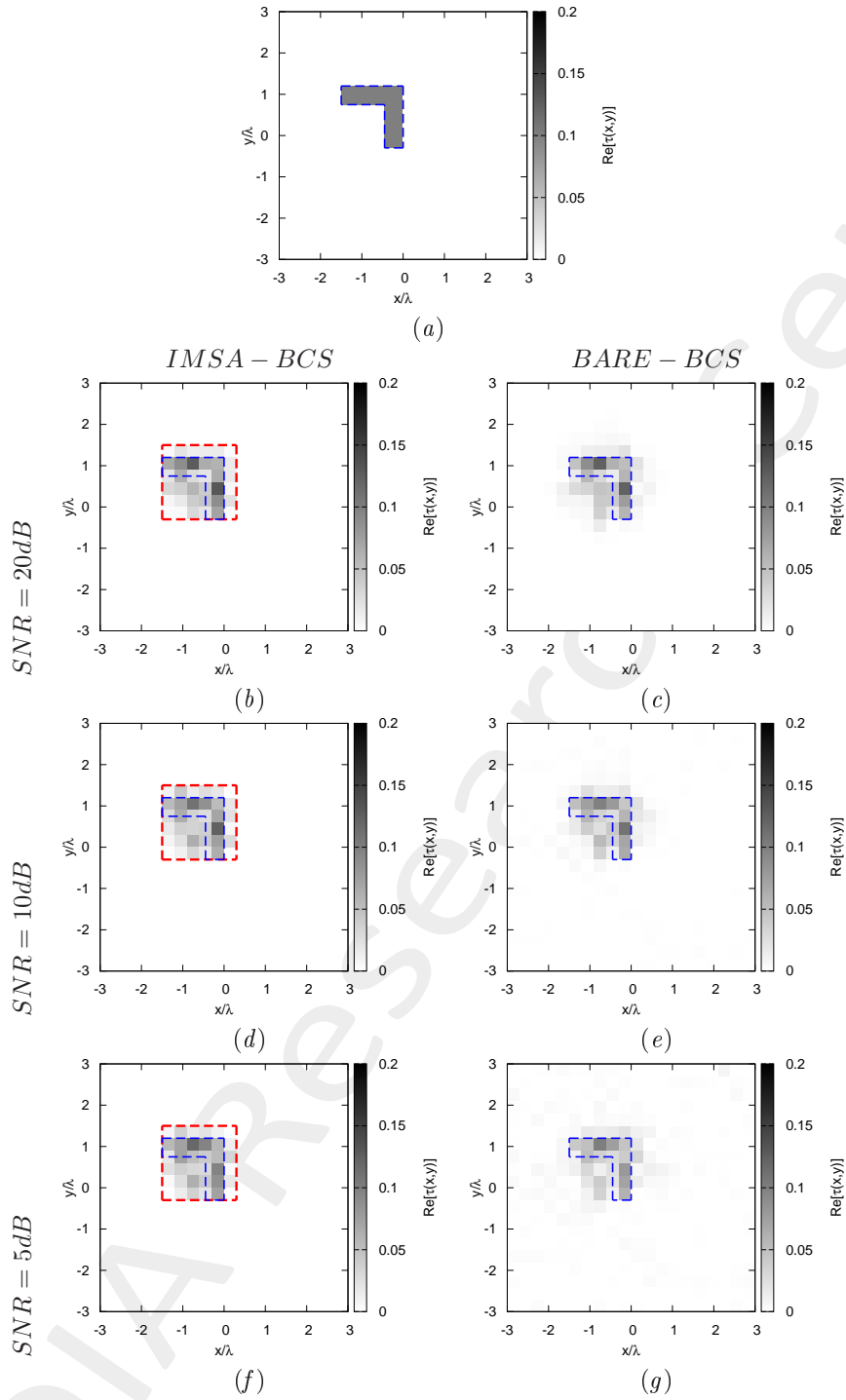


Figure 3: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.10$  - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].

<i>SNR = 50dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$2.36 \times 10^{-3}$	$2.63 \times 10^{-3}$
$\xi_{int}$	$3.50 \times 10^{-2}$	$3.67 \times 10^{-2}$
$\xi_{ext}$	$1.21 \times 10^{-3}$	$1.40 \times 10^{-3}$
<i>SNR = 20dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$2.42 \times 10^{-3}$	$2.88 \times 10^{-3}$
$\xi_{int}$	$3.57 \times 10^{-2}$	$4.02 \times 10^{-2}$
$\xi_{ext}$	$1.25 \times 10^{-3}$	$1.52 \times 10^{-3}$
<i>SNR = 10dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$2.55 \times 10^{-3}$	$3.25 \times 10^{-3}$
$\xi_{int}$	$3.55 \times 10^{-2}$	$3.71 \times 10^{-2}$
$\xi_{ext}$	$1.39 \times 10^{-3}$	$1.86 \times 10^{-3}$
<i>SNR = 5dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$2.47 \times 10^{-3}$	$4.29 \times 10^{-3}$
$\xi_{int}$	$3.22 \times 10^{-2}$	$4.33 \times 10^{-2}$
$\xi_{ext}$	$1.36 \times 10^{-3}$	$2.44 \times 10^{-3}$

Table III: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.10$  - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.



1.1.4 L-shaped Object,  $\ell = 1.5\lambda$ ,  $\tau = 0.15$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

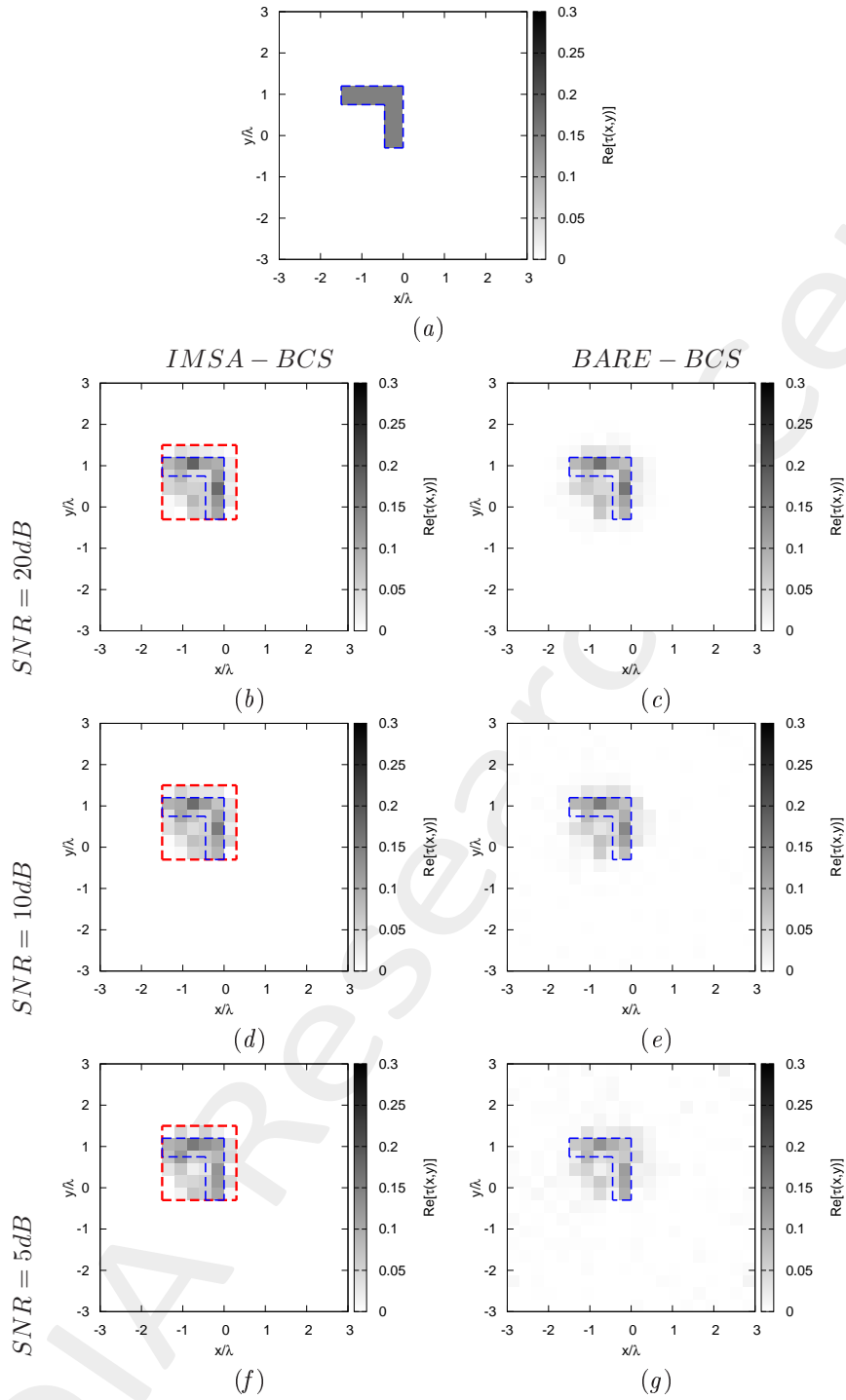


Figure 4: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.15$  - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].

<i>SNR = 50dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$3.48 \times 10^{-3}$	$4.04 \times 10^{-3}$
$\xi_{int}$	$4.62 \times 10^{-2}$	$5.20 \times 10^{-2}$
$\xi_{ext}$	$1.79 \times 10^{-3}$	$2.17 \times 10^{-3}$
<i>SNR = 20dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$3.69 \times 10^{-3}$	$4.38 \times 10^{-3}$
$\xi_{int}$	$4.97 \times 10^{-2}$	$5.50 \times 10^{-2}$
$\xi_{ext}$	$1.92 \times 10^{-3}$	$2.39 \times 10^{-3}$
<i>SNR = 10dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$3.87 \times 10^{-3}$	$5.28 \times 10^{-3}$
$\xi_{int}$	$5.03 \times 10^{-2}$	$5.53 \times 10^{-2}$
$\xi_{ext}$	$2.10 \times 10^{-3}$	$3.00 \times 10^{-3}$
<i>SNR = 5dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$3.85 \times 10^{-3}$	$6.99 \times 10^{-3}$
$\xi_{int}$	$4.50 \times 10^{-2}$	$6.41 \times 10^{-2}$
$\xi_{ext}$	$2.06 \times 10^{-3}$	$3.90 \times 10^{-3}$

Table IV: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.15$  - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.

1.1.5 L-shaped Object,  $\ell = 1.5\lambda$ ,  $\tau = 0.20$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

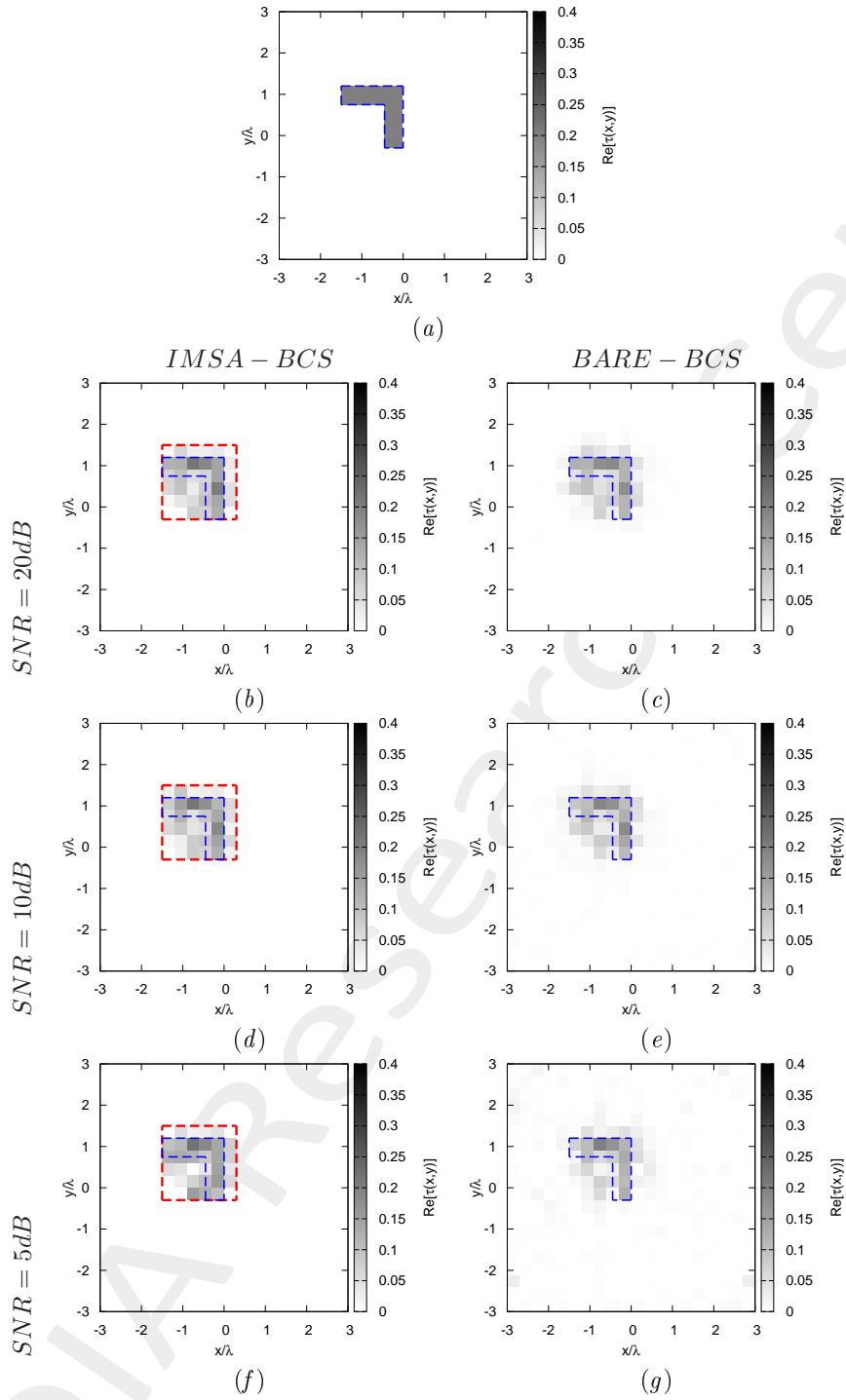
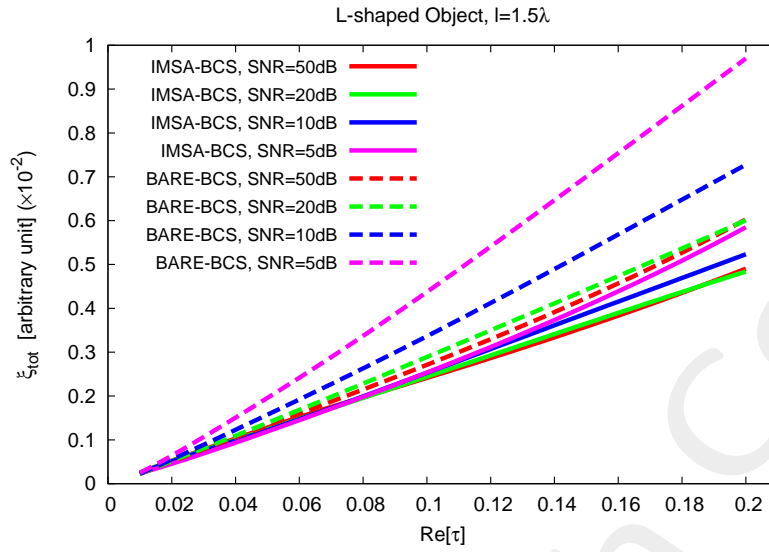


Figure 5: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\ell = 1.5\lambda$ ,  $\tau = 0.20$  - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].

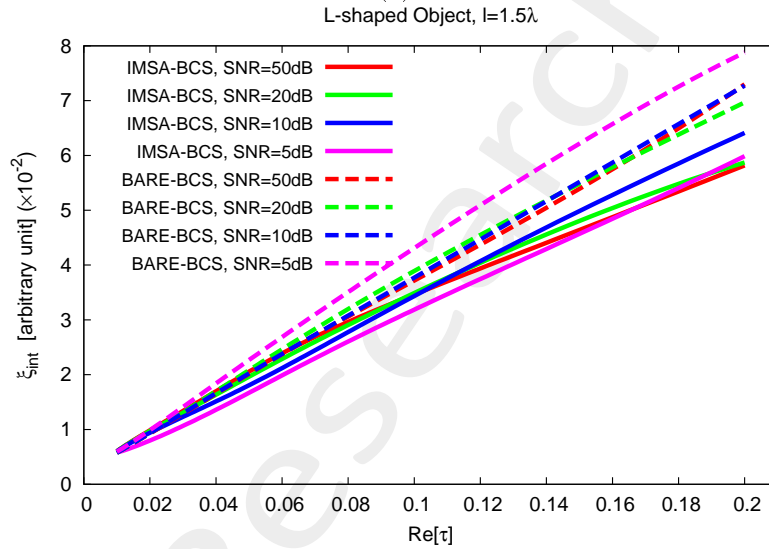
<i>SNR = 50dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$4.90 \times 10^{-3}$	$6.02 \times 10^{-3}$
$\xi_{int}$	$5.81 \times 10^{-2}$	$7.29 \times 10^{-2}$
$\xi_{ext}$	$2.58 \times 10^{-3}$	$3.23 \times 10^{-3}$
<i>SNR = 20dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$4.83 \times 10^{-3}$	$6.00 \times 10^{-3}$
$\xi_{int}$	$5.87 \times 10^{-2}$	$6.96 \times 10^{-2}$
$\xi_{ext}$	$2.51 \times 10^{-3}$	$3.23 \times 10^{-3}$
<i>SNR = 10dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$5.23 \times 10^{-3}$	$7.27 \times 10^{-3}$
$\xi_{int}$	$6.41 \times 10^{-2}$	$7.27 \times 10^{-2}$
$\xi_{ext}$	$2.75 \times 10^{-3}$	$3.98 \times 10^{-3}$
<i>SNR = 5dB</i>		
	<i>IMSA – BCS</i>	<i>BARE – BCS</i>
$\xi_{tot}$	$5.85 \times 10^{-3}$	$9.69 \times 10^{-3}$
$\xi_{int}$	$5.98 \times 10^{-2}$	$7.87 \times 10^{-2}$
$\xi_{ext}$	$3.09 \times 10^{-3}$	$5.25 \times 10^{-3}$

Table V: *L-shaped Object*,  $\ell = 1.5\lambda$ , *IMSA-BCS vs. BARE-BCS*,  $\tau = 0.20$  - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.

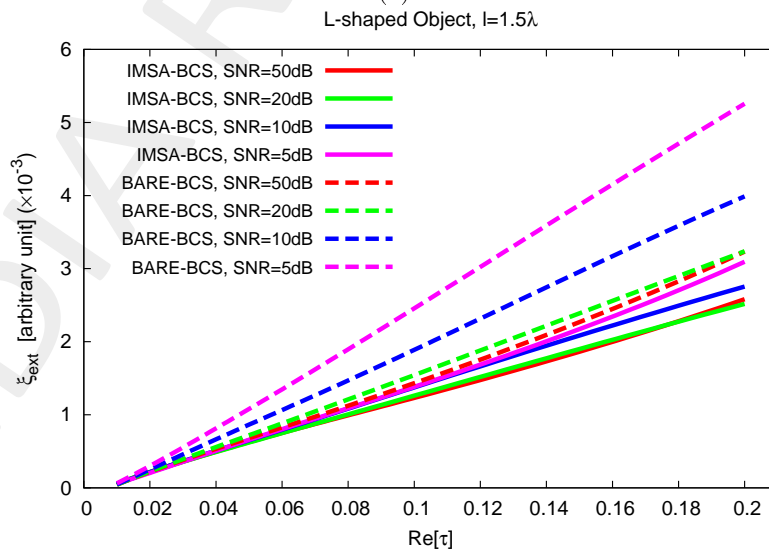
1.1.6 L-shaped Object,  $\ell = 1.5\lambda$  - IMSA-BCS vs. BARE-BCS errors resume vs.  $\tau$



(a)



(b)



(c)

Figure 6: *L-shaped Object*,  $\ell = 1.5\lambda$  - Reconstruction errors vs.  $\tau$ : (a) total error, (b) internal error and (c) external error.

### 1.1.7 L-shaped Object, $\ell = 1.5\lambda$ - IMSA-BCS vs. BARE-BCS errors resume vs. $SNR$

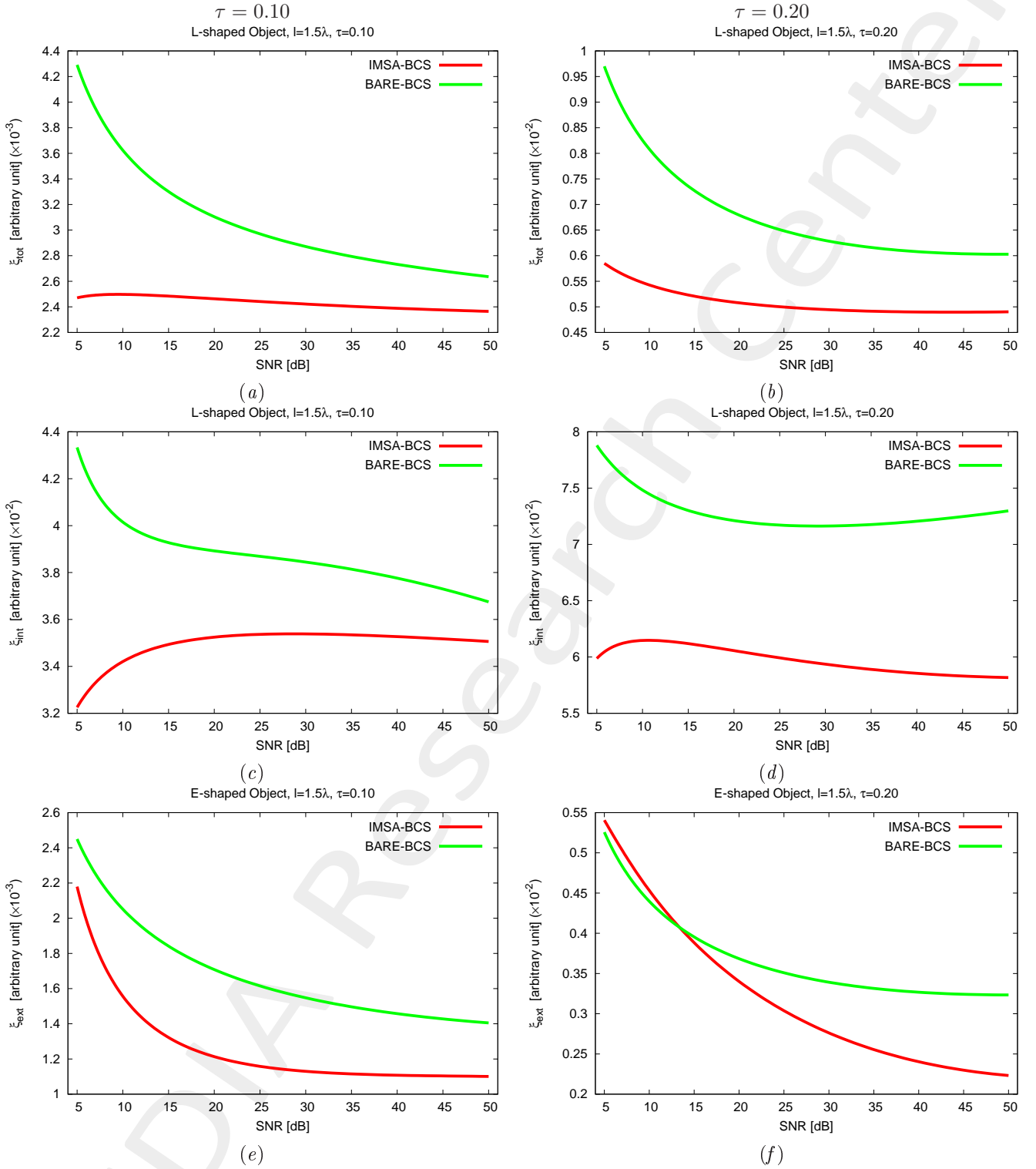


Figure 7: *L-shaped Object*,  $\ell = 1.5\lambda$  - Reconstruction errors vs.  $SNR$ : (a)(b) total error, (c)(d) internal error and (e)(f) external error for (a)(c)(e)  $\tau = 0.10$  and (b)(d)(f)  $\tau = 0.20$ .

## 1.2 Inhomogeneous Square Object, $\ell = 1.5\lambda$

### Test Case Description

#### Direct solver:

- Side of the investigation domain:  $L = 6.0\lambda$
- Cubic domain divided in  $\sqrt{D} \times \sqrt{D}$  cells
- Number of cells for the direct solver:  $D = 1600$  (discretization =  $\lambda/10$ )

#### Investigation domain:

- Cubic domain divided in  $\sqrt{N} \times \sqrt{N}$  cells
- Number of cells for the inversion:
  - First Step IMSA:  $N^{(1)} = 100$  (discretization =  $\lambda/10$ )
  - Following Steps IMSA:  $N^{(i)}$  not fixed, defined according to the estimated  $RoI \mathcal{D}^{(i)}$

#### Measurement domain:

- Total number of measurements:  $M = 60$
- Measurement points placed on circles of radius  $\rho = 4.5\lambda$

#### Sources:

- Plane waves
- Number of views:  $V = 60$ ;  $\theta_{inc}^v = 0^\circ + (v - 1) \times (360/V)$
- Amplitude:  $A = 1.0$
- Frequency:  $F = 300$  MHz ( $\lambda = 1$ )

#### Background:

- $\varepsilon_r = 1.0$
- $\sigma = 0$  [S/m]

#### Scatterer

- Inhomogeneous square object,  $\ell = 1.5\lambda$
- $\varepsilon_r^{(1)} \in \{1.02, 1.04, 1.06, 1.08, 1.10, 1.12, 1.14, 1.16, 1.20\}$  (internal circle)
- $\varepsilon_r^{(2)} = \frac{\varepsilon_r^{(1)}}{2}$  (central circle)
- $\varepsilon_r^{(3)} = \frac{\varepsilon_r^{(1)}}{4}$  (external circle)
- $\sigma = 0$  [S/m]

1.2.1 Inhomogeneous Square Object,  $\ell = 1.5\lambda$ ,  $\tau^{(1)} = 0.02$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

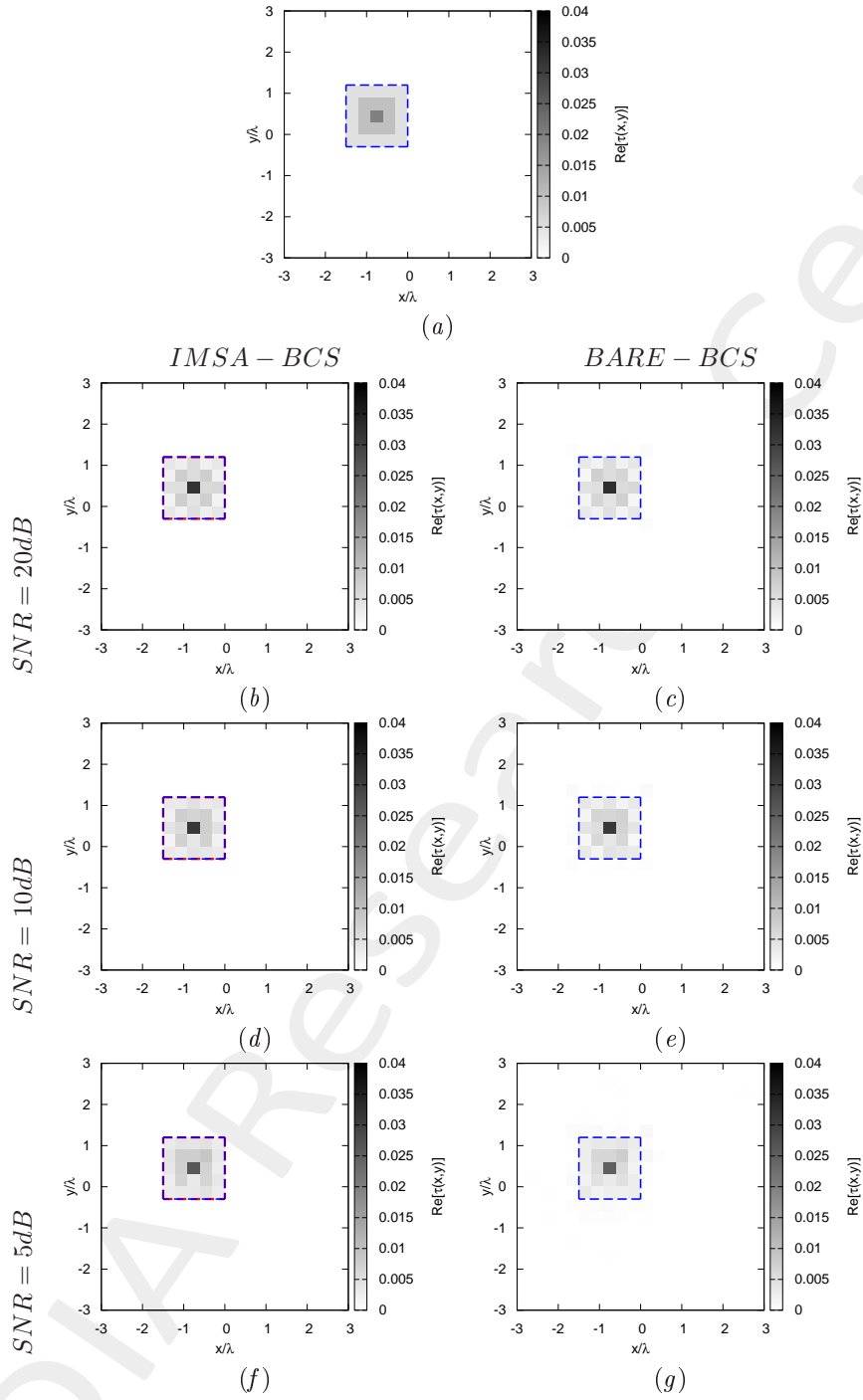


Figure 8: *Inhomogeneous Square Object*,  $\ell = 1.5\lambda$ ,  $\tau^{(1)} = 0.02$  - *IMSA-BCS vs. BARE-BCS* - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].



$SNR = 50dB$		
	$IMSA - BCS$	$BARE - BCS$
$\xi_{tot}$	$1.74 \times 10^{-4}$	$1.93 \times 10^{-4}$
$\xi_{int}$	$2.78 \times 10^{-3}$	$2.95 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$9.06 \times 10^{-6}$
$SNR = 20dB$		
	$IMSA - BCS$	$BARE - BCS$
$\xi_{tot}$	$1.72 \times 10^{-4}$	$1.99 \times 10^{-4}$
$\xi_{int}$	$2.75 \times 10^{-3}$	$3.00 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$1.18 \times 10^{-5}$
$SNR = 10dB$		
	$IMSA - BCS$	$BARE - BCS$
$\xi_{tot}$	$1.58 \times 10^{-4}$	$2.03 \times 10^{-4}$
$\xi_{int}$	$2.53 \times 10^{-3}$	$2.90 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$2.29 \times 10^{-5}$
$SNR = 5dB$		
	$IMSA - BCS$	$BARE - BCS$
$\xi_{tot}$	$1.30 \times 10^{-4}$	$2.42 \times 10^{-4}$
$\xi_{int}$	$2.09 \times 10^{-3}$	$2.91 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$6.12 \times 10^{-5}$

Table VI: *Inhomogeneous Square Object*,  $\ell = 1.5\lambda$ ,  $\tau^{(1)} = 0.02$  - *IMSA-BCS* vs. *BARE-BCS* - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.

1.2.2 Inhomogeneous Square Object,  $\ell = 1.5\lambda$ ,  $\tau^{(1)} = 0.04$  - IMSA-BCS vs. BARE-BCS reconstructed profiles

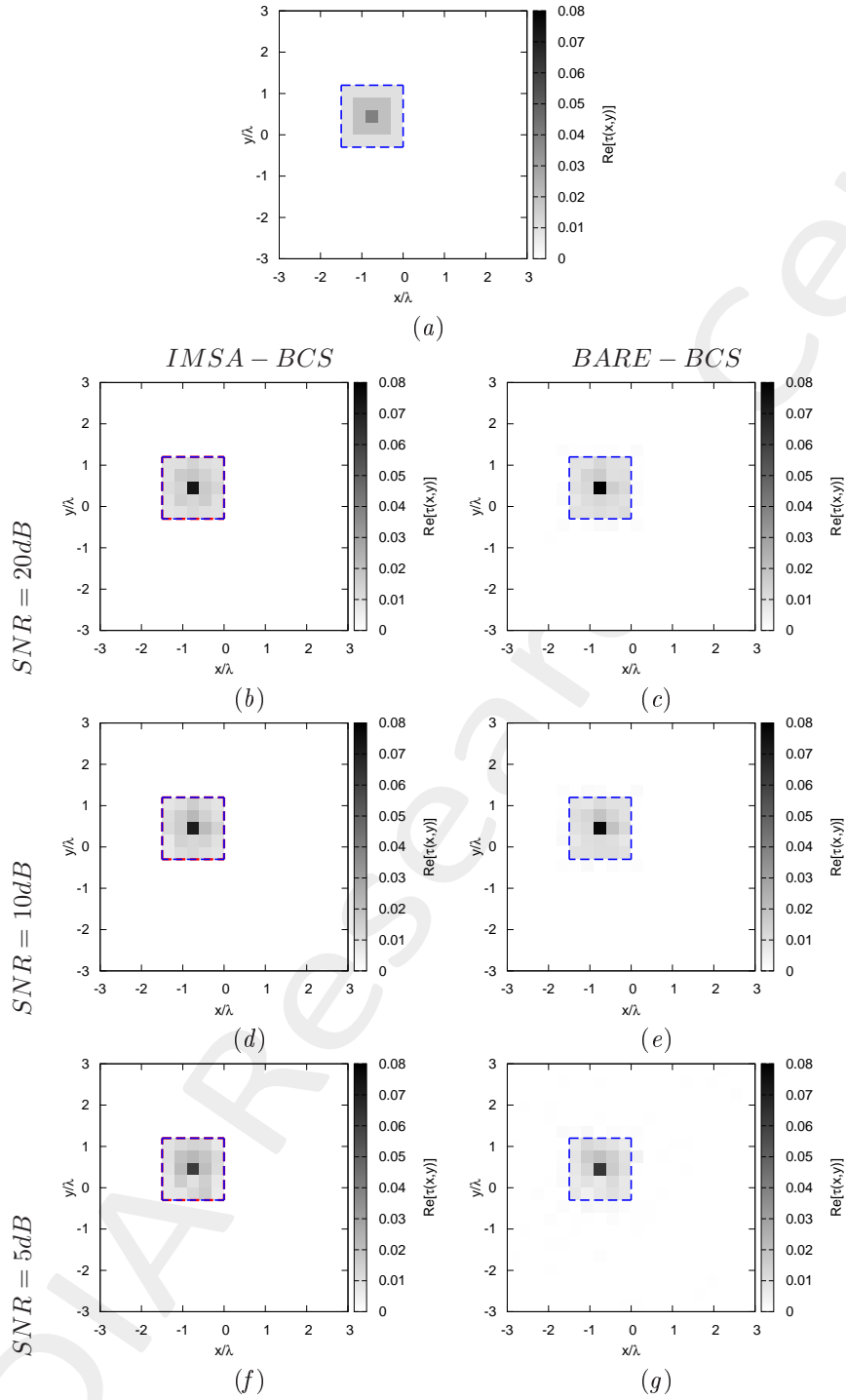


Figure 9: *Inhomogeneous Square Object*,  $\ell = 1.5\lambda$ ,  $\tau^{(1)} = 0.04$  - *IMSA-BCS* vs. *BARE-BCS* - (a) Actual profile, (b)(d)(f) *IMSA-BCS* and *BARE-BCS* reconstructed profiles for (b)(c)  $SNR = 20$  [dB], (d)(e)  $SNR = 10$  [dB] and (f)(g)  $SNR = 5$  [dB].

<i>SNR = 50dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$2.14 \times 10^{-4}$	$3.25 \times 10^{-4}$
$\xi_{int}$	$3.42 \times 10^{-3}$	$4.44 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$5.11 \times 10^{-5}$
<i>SNR = 20dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$2.13 \times 10^{-4}$	$3.27 \times 10^{-4}$
$\xi_{int}$	$3.41 \times 10^{-3}$	$4.44 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$5.28 \times 10^{-5}$
<i>SNR = 10dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$2.33 \times 10^{-4}$	$3.34 \times 10^{-4}$
$\xi_{int}$	$3.72 \times 10^{-3}$	$4.14 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$7.19 \times 10^{-5}$
<i>SNR = 5dB</i>		
	<i>IMSA - BCS</i>	<i>BARE - BCS</i>
$\xi_{tot}$	$2.13 \times 10^{-4}$	$5.09 \times 10^{-4}$
$\xi_{int}$	$3.36 \times 10^{-3}$	$4.20 \times 10^{-3}$
$\xi_{ext}$	$0.00 \times 10^{-1}$	$2.07 \times 10^{-4}$

Table VII: *Inhomogeneous Square Object*,  $\ell = 1.5\lambda$ ,  $\tau^{(1)} = 0.04$  - *IMSA-BCS* vs. *BARE-BCS* - Reconstruction errors: total ( $\xi_{tot}$ ), internal ( $\xi_{int}$ ) and external ( $\xi_{ext}$ ) errors.

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More information on the topics of this document can be found in the following list of references.

## References

- [1] M. Salucci, G. Oliveri, and A. Massa, "GPR prospecting through an inverse scattering frequency-hopping multi-focusing approach," *IEEE Trans. Geosci. Remote Sens.*, vol. 53, no. 12, pp. 6573-6592, Dec. 2015.
  - [2] M. Salucci, L. Poli, N. Anselmi, and A. Massa, "Multifrequency Particle Swarm Optimization for enhanced multiresolution GPR microwave imaging," *IEEE Trans. Geosci. Remote Sens.*, vol. 55, no. 3, pp. 1305-1317, Mar. 2017.
  - [3] M. Salucci, L. Poli, and A. Massa, "Advanced multi-frequency GPR data processing for non-linear deterministic imaging," *Signal Processing*, vol. 132, pp. 306-318, Mar. 2017.
  - [4] N. Anselmi, G. Oliveri, M. Salucci, and A. Massa, "Wavelet-based compressive imaging of sparse targets," *IEEE Trans. Antennas Propag.*, vol. 63, no. 11, pp. 4889-4900, Nov. 2015.
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